Exercise 6

Verify

- (a) the associative law for addition of complex numbers, stated at the beginning of Sec. 2;
- (b) the distributive law (3), Sec. 2.

Solution

Part (a)

The associative law for addition of complex numbers states that

$$(z_1 + z_2) + z_3 = z_1 + (z_2 + z_3).$$

To verify it, let $z_1 = 6i$ and $z_2 = -1 + 2i$ and $z_3 = 2 - 4i$. Check to see whether both sides are equal.

$$[(6i) + (-1+2i)] + (2-4i) \stackrel{?}{=} (6i) + [(-1+2i) + (2-4i)]$$
$$(-1+8i) + 2 - 4i \stackrel{?}{=} 6i + (1-2i)$$
$$1 + 4i = 1 + 4i$$

The associative law for addition is verified.

Part (b)

The distributive law states that

$$z(z_1 + z_2) = zz_1 + zz_2.$$

To verify it, let $z_1 = 6i$ and $z_2 = -1 + 2i$ and z = 3 + 5i. Check to see whether both sides are equal.

$$(3+5i)[(6i) + (-1+2i)] \stackrel{?}{=} (3+5i)(6i) + (3+5i)(-1+2i)$$

$$(3+5i)(-1+8i) \stackrel{?}{=} (18i+30i^2) + (-3+6i-5i+10i^2)$$

$$-3+24i-5i+40i^2 \stackrel{?}{=} 18i-30-3+i-10$$

$$-3+19i-40 \stackrel{?}{=} 19i-43$$

$$-43+19i = -43+19i$$

The distributive law is verified.

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